

General Certificate of Education (A-level) January 2011

Mathematics

MD02

(Specification 6360)

Decision 2

Mark Scheme

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all examiners participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for standardisation each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, examiners encounter unusual answers which have not been raised they are required to refer these to the Principal Examiner.

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Key to mark scheme abbreviations

M	mark is for method
m or dM	mark is dependent on one or more M marks and is for method
A	mark is dependent on M or m marks and is for accuracy
В	mark is independent of M or m marks and is for method and accuracy
E	mark is for explanation
√or ft or F	follow through from previous incorrect result
CAO	correct answer only
CSO	correct solution only
AWFW	anything which falls within
AWRT	anything which rounds to
ACF	any correct form
AG	answer given
SC	special case
OE	or equivalent
A2,1	2 or 1 (or 0) accuracy marks
–x EE	deduct x marks for each error
NMS	no method shown
PI	possibly implied
SCA	substantially correct approach
c	candidate
sf	significant figure(s)
dp	decimal place(s)

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

Q 1	Solution B	Marks	Total	Comments
1	B			
	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	17 3	7 20	H 20 2 23 2 26 22 2 26 26 1 27 26 1 27 20 3 23 26
(a)	Forward pass	M1		up to one slip ft
	Correct	A1		
	Backward pass	M1		up to one slip ft
	Correct	A1	4	
(b)(i)	Critical path A C E G I K L	B1		
(6)(1)	Citacai paai A C E O I K E	D 1		
(ii)	Float for $D = 13 - 2 - 7$	M1		'their 13' - 'their 2' - 7
()	= 4 days	A1	3	
(c)	A C E G I K L correct durations	M1		one slip in duration or height
	and heights	A1		correct
	D and B and F correct (no "holes") H and J correct (no "holes")	B1 B1	4	withhold final mark earned if not clear
	Traile 5 correct (no notes)	D1	4	which activities are taking place at any
				time
	Number 6	F E	14 15 16 17 umber of day	H J J L L 7 18 19 20 21 22 23 24 25 26 27 28 29 30 ys
(d)	Correctly dealing with <i>D</i> , <i>B</i> and <i>F</i>	B1		ft 1 slip
()	Correctly dealing with H and J	B1		ft 1 slip
	Minimum extra time = 3 days	B1	3	CAO
	may be interchanged		TITI	
	8			May be
	Number 6 B D	F		interchanged
	of workers 5			other possibilities
	3 A C E		c	I = I
	1	\overline{F}	G	
	0 1 2 3 4 5 6 7 8 9 10 11 12 13 14	15 16 17 18	19 20 21 22	23 24 25 26 27 28 29 30
	Num	ber of days		
	Total		14	

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MD02 (cont Q)		Solution			Marks	Total	Comments
$\frac{Q}{Q(a)(i)}$			Solution			Widiks	Total	Comments
` , , , ,	4	8	12	2	6			
	0	5	12	4	8			
	11	10	8	3	8			
	2	9	3	5	1			
						D1	1	
	n	n	n	n	n	B1	1	
(ii)	Hungari 20 – x g	ows = no an algori ives mea eeds min	thm mini	imises	ot met	E1 E1 E1	3	square matrix by adding extra row (total score) points lost (in each entry)
(b)(i)	2 0 8	6 5 7 8	10 12 5 2	0 4 0	4 8 5	M1		reducing rows column reduction leaves matrix unchanged
						A1√	2	(p = 4, q = 5)
	V	0	0	V		A1√	2	(ft one slip)
(ii)	Zeros co	overed wi	ith 4 line	s <u>shown</u>	<u>1</u>	B1		row 5 and columns 1, 4 and 5
	2 0 8 ——————————————————————————————————	4 3 5	8 10 3 — 0	0 4 0 4	4 8 5 ————	M1		subtract 2 from all uncovered and add 2 to double covered (condone one slip)
		0	0	-		A1		(follow through their p and q)
						M1		augment (at least) one more time
	2	1	5	\bigcirc	1			(condone one slip)
	8 4 5	0 2 6 0	7 0 0	4 0 7 5	5 2 0 2	A1		may put line through second row and not first column $ \begin{array}{ccccccccccccccccccccccccccccccccccc$
			_					be covered by 5 lines
	1D, 2A,	3C, 4E i	s matchi	ng		B1	6	(field B unused)
(iii)	(18 + 20) + 12 + 1	19 =) 69			B1	1	
	l				Total	1	12	

13

Total

MD02	(cont)

MD02 (cont	Solution	Marks	Total	Comments
3(a)(i)	Row minima $2, -3, x$	B1	1	Comments
(ii)	Column maxima 3, 6, 4	B1	1	Check for answers written on table
	Max (row min) = 2 Min (col max) = 3 Or $2 \neq 3$	M1		Condone Best (worst) =2 etc Worst (best) =3
	Since $2 \neq 3 \rightarrow$ no stable solution	A1cso	3	Both lines and statement must score previous B1, B1
(b)	$\begin{cases} x < 2, x + 3 < 6, 3 < 4 \\ \rightarrow R_1 \text{ dominates } R_3 \end{cases}$ Either of these	В1	1	hence Rhona should not play R ₃
(c)(i)	Let Rhona play R_1 with prob p and R_2 with prob $1-p$			
	When C plays C_1 : exp value = $2p + 3(1 - p)$ C_2 : $6p - 3(1 - p)$			= 3 - p $= -3 + 9 p$
	$C_3: 4p - (1-p) = -1 + 5p$	M1 A1		any two correct unsimplified all correct unsimplified
	3	M1		drawing two of their expected values for $0 \le p \le 1$ both vertical axes using same scale condone use of horizontal lines in paper
	-1 0 1 p	A1		all three correct lines must see numbers on at least one vertical axis
	3-p = -1+5p	M1		choosing highest point of region
	$\rightarrow p = \frac{2}{3}$	A1		
	\rightarrow Rhona plays R ₁ $\frac{2}{3}$ of time			
	and $R_2 = \frac{1}{3}$ of time	E1√	7	ft their p
(ii)	Value of game = $3 - \frac{2}{3} = \frac{7}{3}$	B1	1	or $-1 + \frac{10}{3} = \frac{7}{3}$
	Total		13	

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MD02 ((cont)

MD02 (cont		,		
Q	Solution	Marks	Total	Comments
4(a)(i)	$\frac{4}{-1} = -4$; $\frac{10}{2} = 5$; $\frac{21}{4} = 5\frac{1}{4}$ 5 is smallest positive ratio	E1		Must see 5 and $5\frac{1}{4}$ plus correct statement
	Pivot = 2	B1	2	
(ii)	1 0 $-\frac{1}{2}$ 5 0 $\frac{3}{2}$ 0 15	M1		row operations (even with wrong pivot)
	$0 0 \frac{3}{2} 3 1 \frac{1}{2} 0 9$	A1		1st, 2nd or last row correct
	$0 1 \frac{1}{2} 2 0 \frac{1}{2} 0 5$	A1		another of these correct
	0 0 0 -5 0 -2 1 1	A1		all correct (condone multiples of rows)
	Negative value in top row (→ optimum not reached)	E1	5	must have negative value in their top row
(b)(i)	New pivot is 'their $\frac{3}{2}$ ' in y-column PI	M1		or multiple of this
	1 0 0 6 $\frac{1}{3}$ $\frac{5}{3}$ 0 18	A1		1st, 3rd or 4th row correct
	$0 0 1 2 \frac{2}{3} \frac{1}{3} 0 6$	A1		another of these rows correct
	$0 1 0 1 -\frac{1}{3} \frac{1}{3} 0 2$			
	0 0 0 -5 0 -2 1 1	A1	4	all correct (condone multiples of rows)
(ii)	Optimum value of <i>P</i> reached	E1		must have no negative values in top row
	P = 18	B1√		ft their tableau
	x = 2, y = 6, z = 0	B1√		s = 0, $t = 0$, $u = 1(no more than 2 slips in final tableau for ft)$
	$4x + 2y + 3z \le 21$ still has slack	B1	4	Tableau must indicate <i>u</i> is only slack variable
	Total		15	

MD02 (cont)

MD02 (cont		N/ 1	TD 4 1			<u> </u>		
Q	Solution	Marks	Total	Comments				
5(a)				Stage	State	From	Value	
				1	I	T	-7	
					J	T	-6	
					K	T	-5	
	Completing stage 2 values (condone			2	Е	I	-7 - 4 = -11	←
	correct unsimplified) (all 7 values)	B1			F	I	-7 - 3 = -10	←
						J	-6 - 2 = -8	
					G	I	-7 + 4 = -3	
						J	-6 + 7 = 1	
						K	-5 - 1 = -6	\leftarrow
					Н	K	-5 + 4 = -1	←
	At least 6 values calculated at stage 3	M1		3	A	Е	-11 + 5 = -6	
	(M0 for 10 or more values)					G	-6 - 2 = -8	←
	Using only their minimum F or G value				В	Е	-11 - 2 = -13	
	from stage 2	m1				F	-10-4=-14	\leftarrow
	110111 54480 2	1111			С	F	-10 + 6 = -4	
						G	-6 - 3 = -9	\leftarrow
	All 9 stage 3 values correct	A1				Н	-1 - 5 = -6	
	All 9 stage 3 values correct				D	G	-6 - 5 = -11	\leftarrow
	Heimannining (at least 2) forms A. B. C. D.					Н	-1 - 3 = -4	
	Using minima (at least 3) from A, B, C, D	3.71		4	S	A	-8 + 23 = 15	
	stage 3 in stage 4	M1			~	В	-14 + 28 = 14	←
			_			С	-9 + 25 = 16	
	All correct in stage 4	A1	6			D	-11 + 25 = 14	←
(b)	Minimum cost of ticket (£)14	B1√		ft their	lowest s	stage 4 v	alue	
	Path SBFIT	B1		one cor	rect patl	h		
	SDTTT $SDGKT$	B1	3			h and no	others	
	Total	Di	9	2110 001	.ioci pat	ii aiia iic	, outers	
	Total		7					

D02 (cont				<u></u>
Q	Solution	Marks	Total	Comments
6(a)	<i>SP</i> ≥12			
	$SQ \ge 10$			
	<i>SR</i> ≥ 17	B1		S in correct place, (arrows) and capacities
	<i>YT</i> ≥ 18			
	<i>ZT</i> ≥17	B1	2	T in correct place, (arrows) and capacities
				* * * * * * * * * * * * * * * * * * * *
(b)	SPUYT 10	B1		
	SRVWZT 8	B1	2	
(c)(i)	Initial flow forward and backward			
	PU 2 and 10; UY 0 and 10	B1	_	
	RV 0 and 8; VW 1 and 8; WZ 2 and 8	B1	2	withhold one B1 if paths to <i>S</i> and <i>T</i> not updated
(ii)	Two correct routes and flows on Figure 6	M1		SPUYT 10
()	5			SRYWZT 8
	Correct additional flows			SPUXYT 2
	Max flow = 33	A1		SQVUXYT 6
				SRWXZT 5
	Adjustment of at least 4 edges corresponding to flows (forward and	M1		SRWZT 2
	backward)	WH		(other possibilities
	Correct final flows forward and backward	A1cso	4	edges <i>UY</i> , <i>UX</i> , <i>WX</i> and <i>WZ</i> will be
	(must score A1 for table)	111000	•	saturated
	, ,			XY + XZ = 13 in back flow
(d)	Cut with value 33 is through	B1	1	
(4)	UY, UX, WX and WZ	D 1	•	
	Total		11	
	TOTAL		75	