# General Certificate of Education (A-level) January 2011 

## Mathematics

MD02

## (Specification 6360)

Decision 2

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all examiners participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for standardisation each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, examiners encounter unusual answers which have not been raised they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

## Further copies of this Mark Scheme are available from: aqa.org.uk

Copyright © 2011 AQA and its licensors. All rights reserved.

## Copyright

AQA retains the copyright on all its publications. However, registered centres for AQA are permitted to copy material from this booklet for their own internal use, with the following important exception: AQA cannot give permission to centres to photocopy any material that is acknowledged to a third party even for internal use within the centre.

Set and published by the Assessment and Qualifications Alliance.

## Key to mark scheme abbreviations

| M | mark is for method |
| :--- | :--- |
| m or dM | mark is dependent on one or more M marks and is for method |
| A | mark is dependent on M or m marks and is for accuracy |
| B | mark is independent of M or m marks and is for method and accuracy |
| E | mark is for explanation |
| Jor ft or F | follow through from previous incorrect result |
| CAO | correct answer only |
| CSO | correct solution only |
| AWFW | anything which falls within |
| AWRT | anything which rounds to |
| ACF | any correct form |
| AG | answer given |
| SC | special case |
| OE | or equivalent |
| A2,1 | 2 or 1 (or 0) accuracy marks |
| $-x$ EE | deduct $x$ marks for each error |
| NMS | no method shown |
| PI | possibly implied |
| SCA | substantially correct approach |
| c | candidate |
| sf | significant figure(s) |
| dp | decimal place(s) |

## No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award full marks. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn no marks.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns full marks, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains no marks.

## Otherwise we require evidence of a correct method for any marks to be awarded.



MD02 (cont)


## MD02 (cont)

| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 3(a)(i) | Row minima 2, $-3, x$ | B1 | 1 |  |
| (ii) | Column maxima 3, 6, 4 | B1 |  | \} Check for answers written on table |
|  | $\begin{aligned} & \operatorname{Max}(\text { row } \min )=2 \\ & \operatorname{Min}(\text { col } \max )=3 \end{aligned} \quad \text { Or } 2 \neq 3$ | M1 |  | $\begin{gathered} \text { Condone Best (worst) }=2 \text { etc } \\ \text { Worst (best) }=3 \end{gathered}$ |
|  | Since $2 \neq 3 \rightarrow$ no stable solution | A1cso | 3 | Both lines and statement must score previous B1, B1 |
| (b) | $\left.\begin{array}{l}x<2, x+3<6,3<4 \\ \rightarrow \mathrm{R}_{1} \text { dominates } \mathrm{R}_{3}\end{array}\right\}$ Either of these | B1 | 1 | hence Rhona should not play $\mathrm{R}_{3}$ |
| (c)(i) | Let Rhona play $\mathrm{R}_{1}$ with prob $p$ and $\mathrm{R}_{2}$ with prob $1-p$ |  |  |  |
|  | When C plays $\begin{aligned} & \mathrm{C}_{1}: \exp \text { value }=2 p+3(1-p) \\ & \mathrm{C}_{2}: 6 p-3(1-p) \end{aligned}$ |  |  | $\begin{aligned} & =3-p \\ & =-3+9 p \end{aligned}$ |
|  | $\mathrm{C}_{3}: 4 p-(1-p)=-1+5 p$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \end{gathered}$ |  | any two correct unsimplified all correct unsimplified |
|  |  | M1 |  | drawing two of their expected values for $0 \leq p \leq 1$ <br> both vertical axes using same scale condone use of horizontal lines in paper |
|  |  | A1 |  | all three correct lines must see numbers on at least one vertical axis |
|  | $\begin{aligned} & 3-p=-1+5 p \\ & \rightarrow p=\frac{2}{3} \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ |  | choosing highest point of region |
|  | $\rightarrow$ Rhona plays $\mathrm{R}_{1} \frac{2}{3}$ of time and $\mathrm{R}_{2} \frac{1}{3}$ of time | E1 $\checkmark$ | 7 | ft their $p$ |
| (ii) | Value of game $=3-\frac{2}{3}=\frac{7}{3}$ | B1 | 1 | $\text { or }-1+\frac{10}{3}=\frac{7}{3}$ |
|  | Total |  | 13 |  |


| $\begin{aligned} & \text { MD02 (cont) } \\ & \hline \mathbf{Q} \\ & \hline \end{aligned}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Solution |  | Marks | Total | Comments |
| 4(a)(i) | $\frac{4}{-1}=-4 ; \frac{10}{2}=5 ; \frac{21}{4}=5 \frac{1}{4}$ <br> 5 is smallest positive ratio <br> Pivot $=2$ |  | E1 B1 | 2 | Must see 5and $5 \frac{1}{4}$ plus correct statement |
| (ii) | $\begin{array}{llllllll}1 & 0 & -\frac{1}{2} & 5 & 0 & \frac{3}{2} & 0\end{array}$ | 15 | M1 |  | row operations (even with wrong pivot) |
|  | $\begin{array}{lllllll}0 & 0 & \frac{3}{2} & 3 & 1 & \frac{1}{2} & 0\end{array}$ |  | A1 |  | 1st, 2nd or last row correct |
|  | $\begin{array}{llllllll}0 & 1 & \frac{1}{2} & 2 & 0 & \frac{1}{2} & 0\end{array}$ | 5 | A1 |  | another of these correct |
|  | $\begin{array}{llllllll}0 & 0 & 0 & -5 & 0 & -2 & 1\end{array}$ | 1 | A1 |  | all correct (condone multiples of rows) |
|  | Negative value in top row ( $\rightarrow$ optimum not reached) |  | E1 | 5 | must have negative value in their top row |
| (b)(i) | New pivot is 'their $\frac{3}{2}$ ' in $y$-column PI |  | M1 |  | or multiple of this |
|  | $\begin{array}{llllllll}1 & 0 & 0 & 6 & \frac{1}{3} & \frac{5}{3} & 0\end{array}$ |  | A1 |  | 1st, 3rd or 4th row correct |
|  | $\begin{array}{llllllll}0 & 0 & 1 & 2 & \frac{2}{3} & \frac{1}{3} & 0\end{array}$ | 6 | A1 |  | another of these rows correct |
|  | $\begin{array}{llllllll}0 & 1 & 0 & 1 & -\frac{1}{3} & \frac{1}{3} & 0\end{array}$ |  |  |  |  |
|  | $\begin{array}{lllllll}0 & 0 & 0 & -5 & 0 & -2 & 1\end{array}$ | 1 | A1 | 4 | all correct (condone multiples of rows) |
| (ii) | Optimum value of $P$ reached |  | E1 |  | must have no negative values in top row |
|  | $P=18$ |  | B1 $\checkmark$ |  | ft their tableau |
|  | $x=2, y=6, z=0$ |  | B1 $\checkmark$ |  | $s=0, t=0, u=1$ |
|  |  |  |  |  | (no more than 2 slips in final tableau for ft ) |
|  | $4 x+2 y+3 z \leq 21$ still has slack |  | B1 | 4 | Tableau must indicate $u$ is only slack variable |
|  |  | Total |  | 15 |  |

MD02 (cont)


## MD02 (cont)



